



# $Z'$ bosons from $E_6$ : collider and electroweak constraints

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- ✦  $Z'$  physics at hadron colliders
- ✦ towards an integrated  $Z'$  analysis
- ✦ based on work in collaboration with  
Paul Langacker, Shoaib Munir and Eduardo Rojas



why care about  $Z'$  bosons?



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- ✧ diagnostics: charges can hint at underlying principles



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- $Z' = \cos\alpha \cos\beta Z_\chi + \sin\alpha \cos\beta Z_\gamma + \sin\beta Z_\psi$   
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- ✧ classification in progress *JE, E. Rojas, 2011*



# $Z'$ charges in $E_6$ models

l	$\nu$		$-2C_2$	$-C_3$	$\bar{\nu}$	$-C_1$	$+C_2$	$+2C_3$
	$e^-$				$e^+$	$+C_1$	$+C_2$	$+2C_3$
q	u			$+C_3$	$\bar{u}$	$-C_1$	$-C_2$	
	d				$\bar{d}$	$+C_1$	$-C_2$	
L	N	$-C_1$	$+C_2$	$-C_3$	D			$-2C_3$
	$E^-$				$\bar{D}$		$+2C_2$	
$\bar{L}$	$E^+$	$+C_1$	$+C_2$	$-C_3$	S		$-2C_2$	$+2C_3$
	$\bar{N}$							



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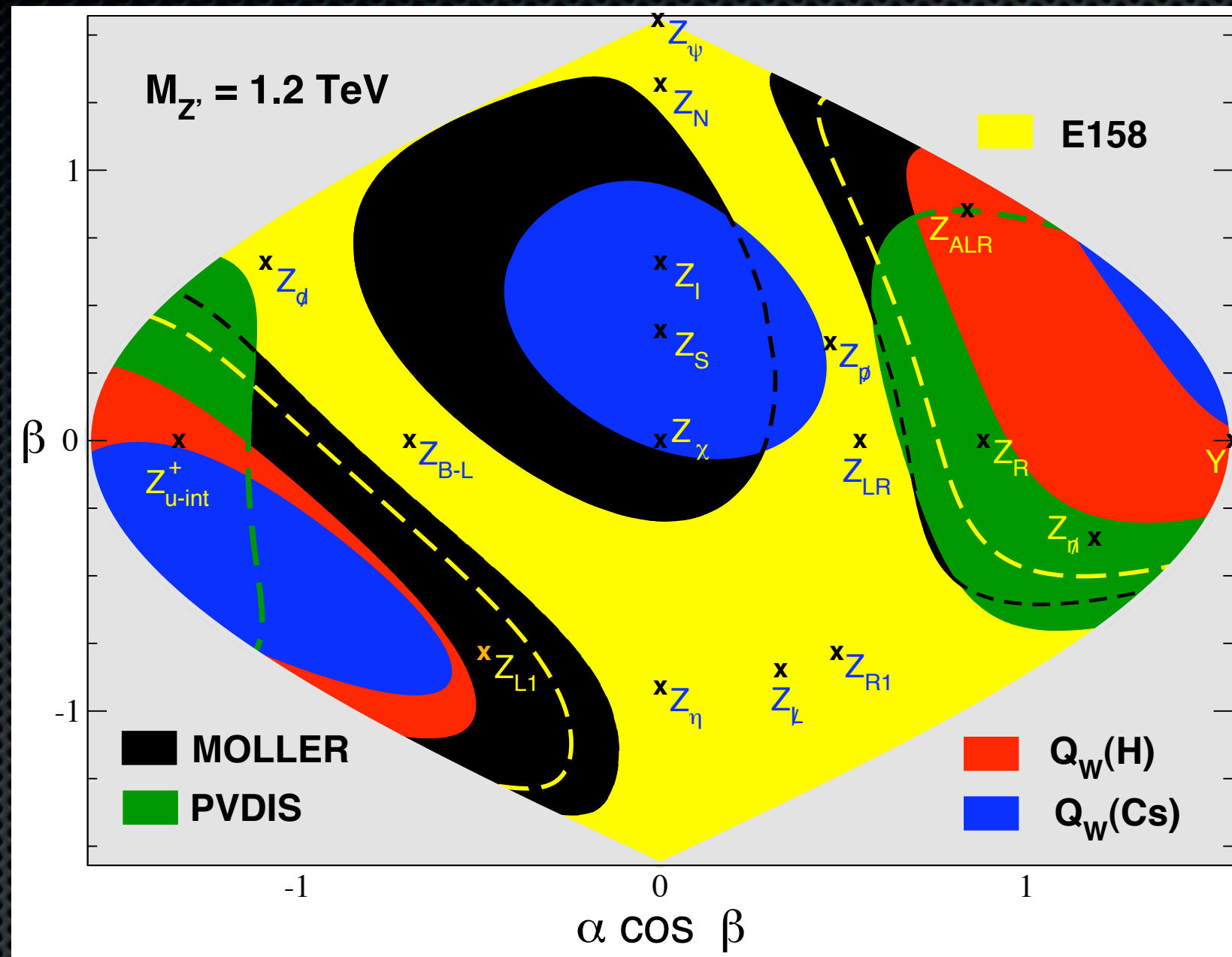


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- ✦ gauge coupling unification
- ➔ the  $U(1)'$  forbids dimension 4 proton decay





# E<sub>6</sub> models & parity violation

E158, MOLLER, Qweak, SOLID, APV



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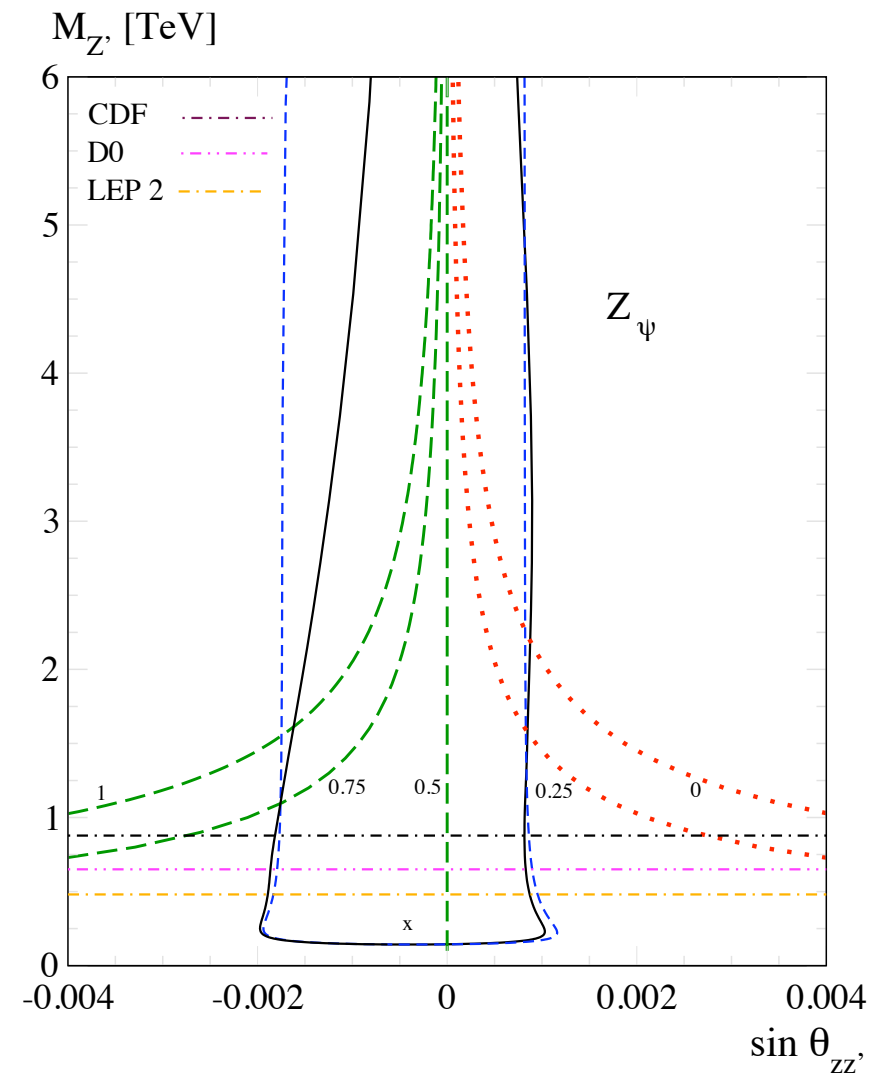
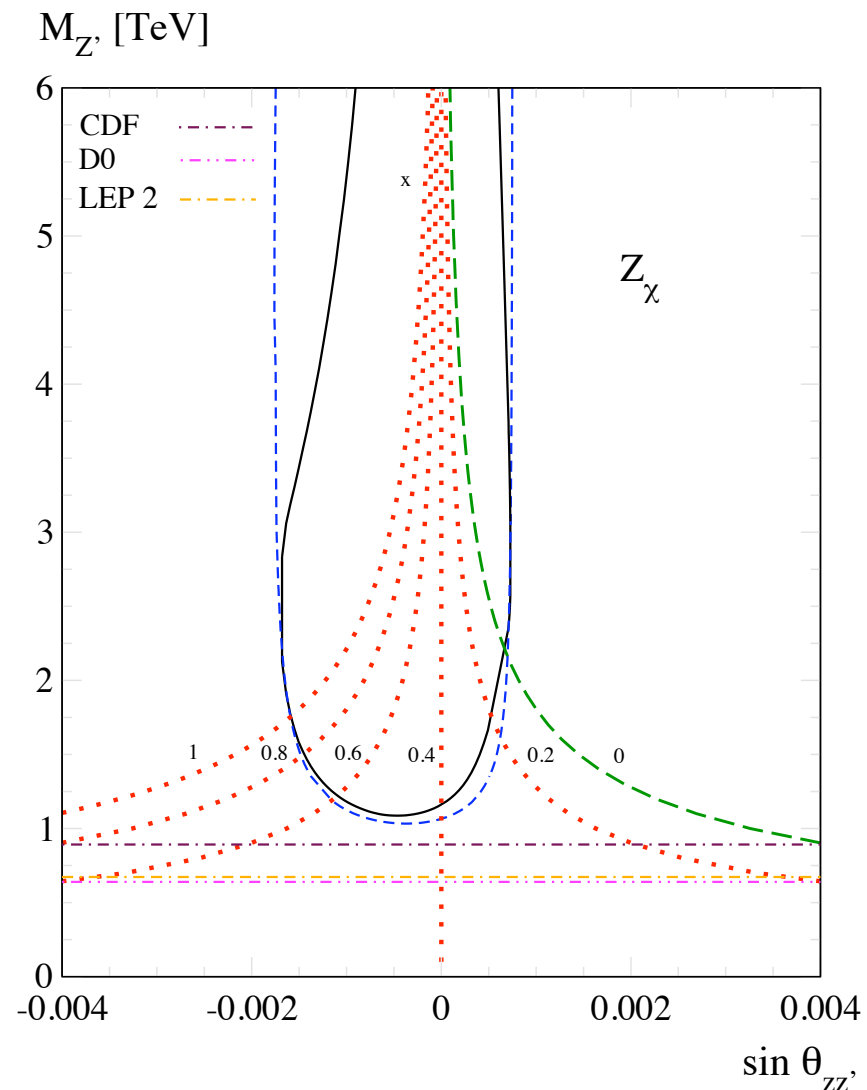
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- simultaneously constrain  $U(1)'$  breaking Higgs sector
- often raises preferred fit range of  $M_H$  relative to SM (cf. NMSSM) *JE, P. Langacker, S. Munir, E. Rojas, JHEP 0908, 017 (2009)*





# Global electroweak fit

Z lineshape, heavy flavor, Z pole asymmetries,  $m_t$ ,  $M_W$ ,  $\nu$ -DIS, APV, polarized electron scattering



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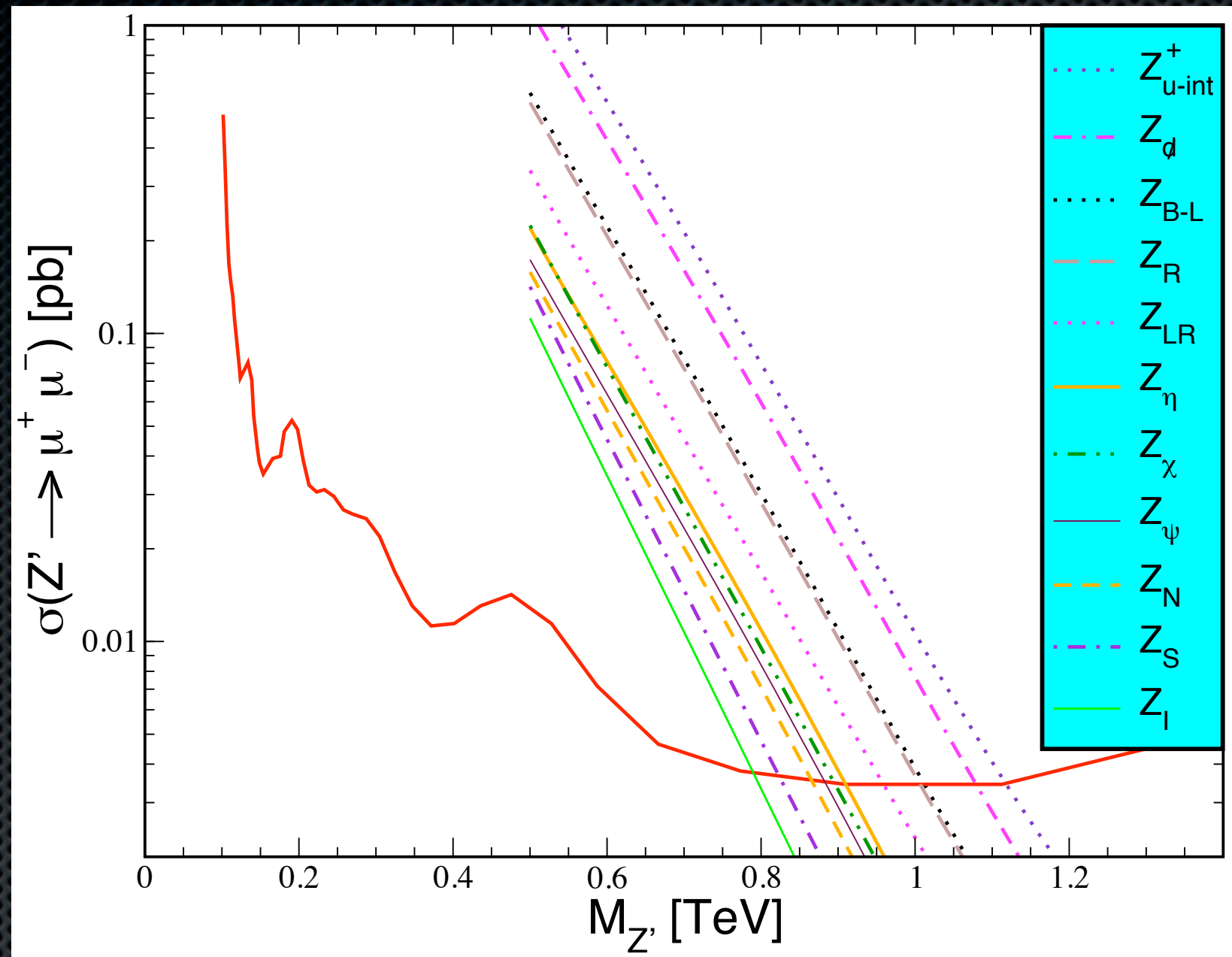
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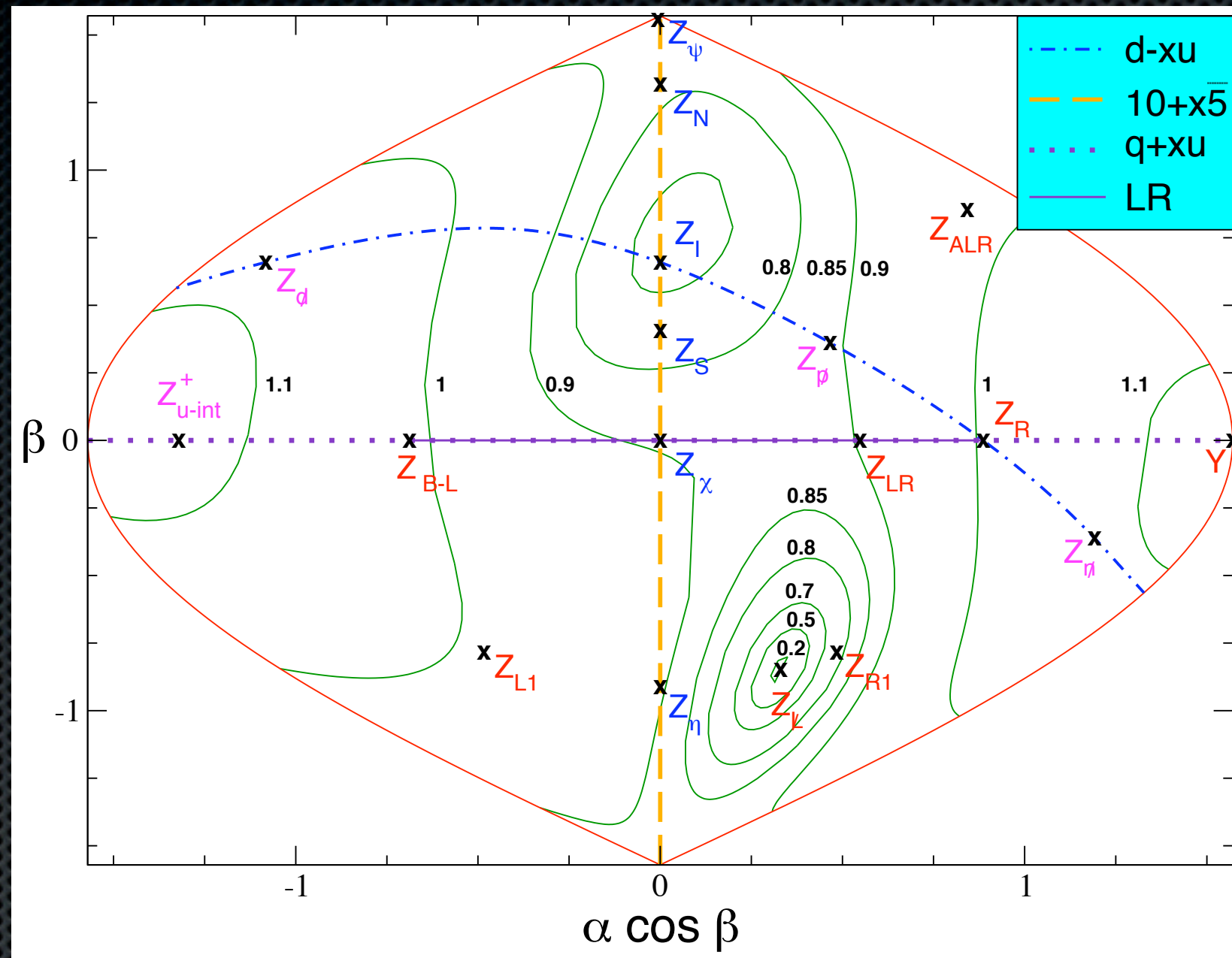




# CDF style analysis

Good agreement with CDF model lines.  
Several additional models included.



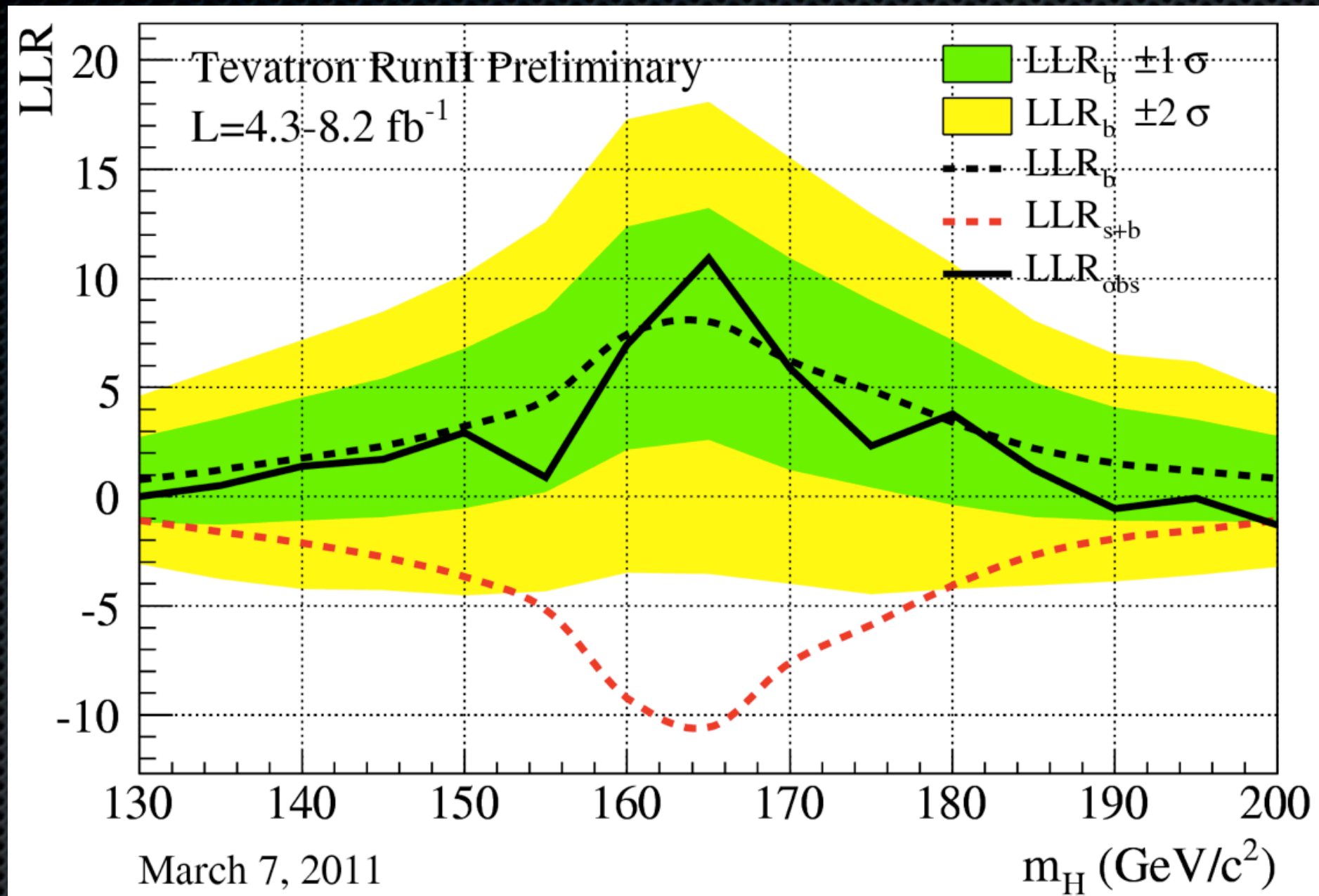


# $E_6$ inspired models

horizontal line:  $SO(10)$  (including left-right) models

vertical line: no kinetic mixing; blue line:  $U(1)_{d-xu}$

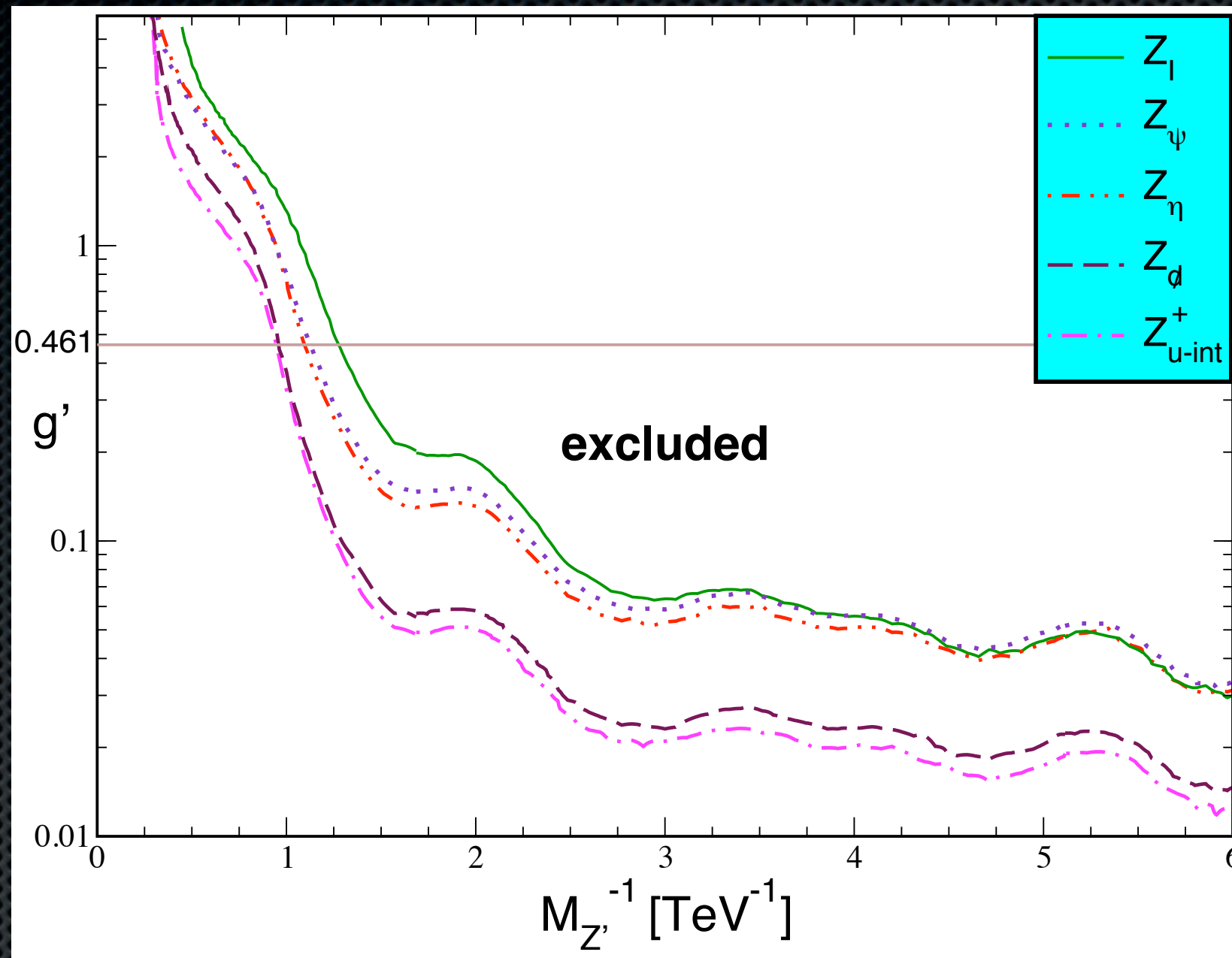




example LLR

Higgs boson search at the Tevatron

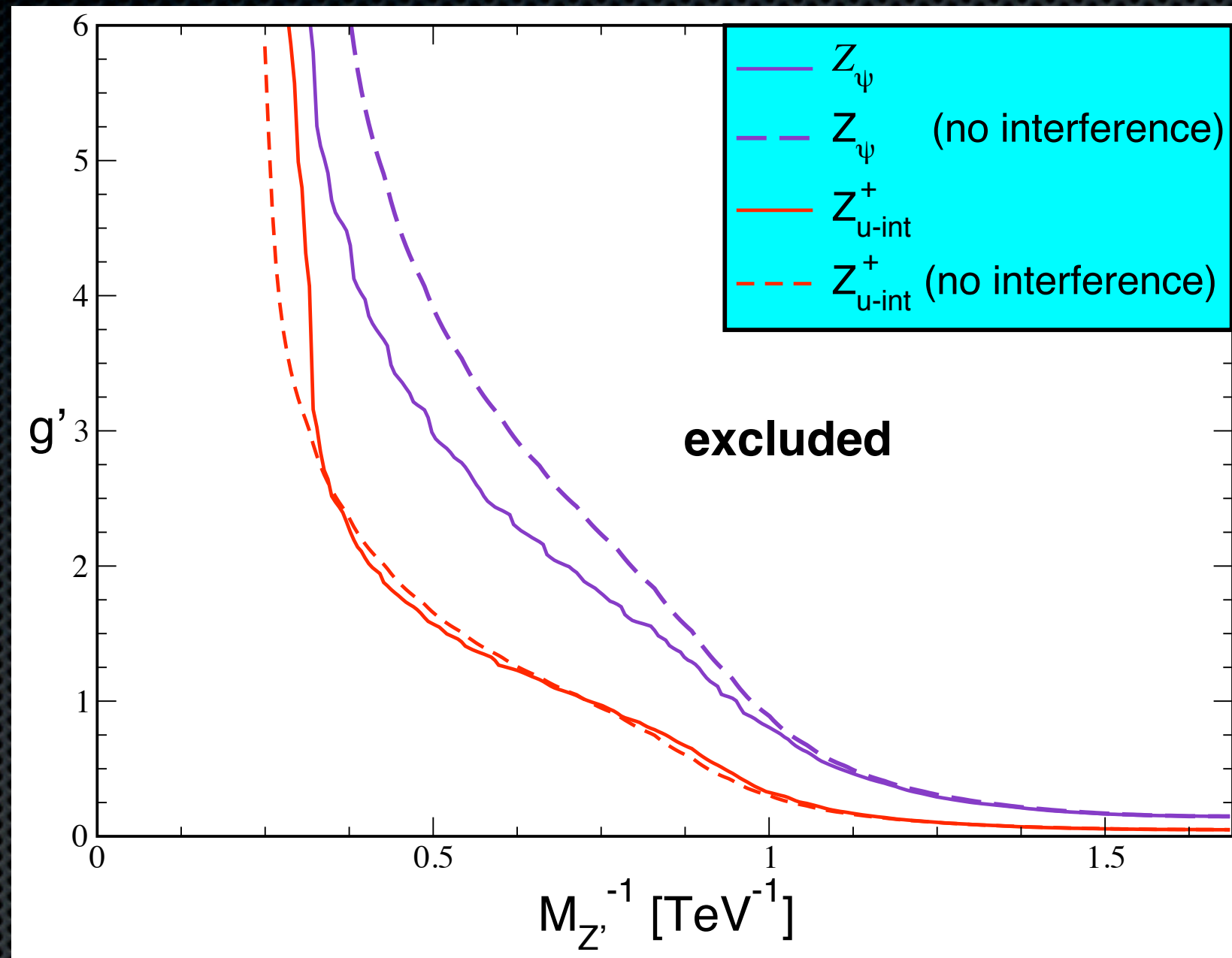




# Bayesian style analysis

$$\Delta\chi^2 = -2 \ln p(\text{data}|\text{s+b}) / p(\text{data}|\text{b}) < 5.99$$

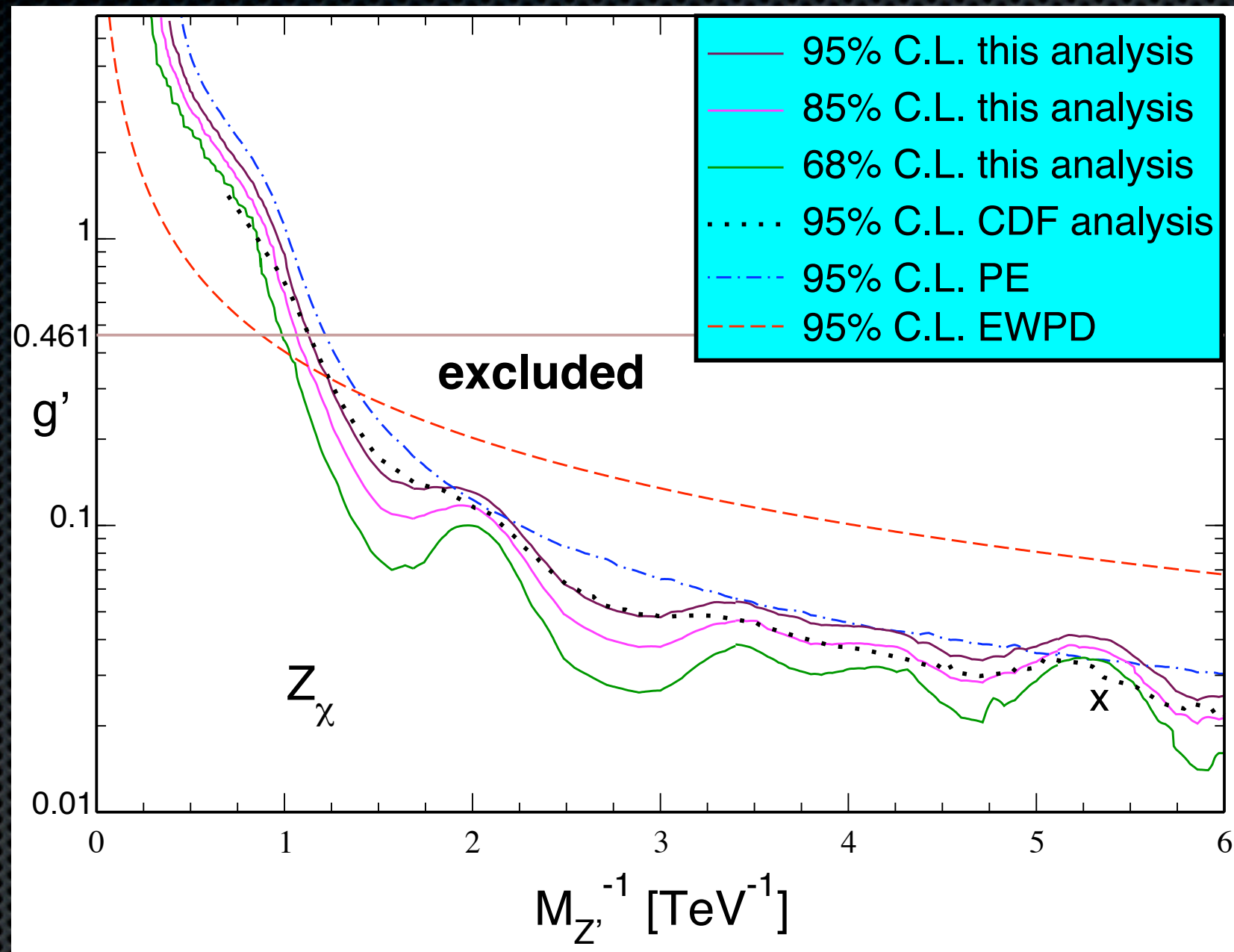




# Interference effects

$Z_{u-int}^{+} \approx -76^{\circ}$ ,  $\beta = 0$  ( $Z_{\psi}$ ) maximizes constructive  $\gamma Z'$  (destructive  $ZZ'$ ) interference for u-quarks





Comparative analysis of  $Z_{\chi}$   
 Complementarity of electroweak precision data  
 and di-lepton channel analyses.



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- **long-term project:** suggests close collaboration between theorists (us) and experimentalists



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- ✧ hadron colliders: complicated constraints in  $g'$  vs.  $M_{Z'}$
- ✧ closer **collaboration** between experimentalists and theorists warranted



# $Z'$ bosons from $E_6$ : collider and electroweak constraints (Jens Erler)

$\alpha = 0$ : no kinetic mixing

$\beta = 0$ :  $SO(10)$

current & future  
low energy constraints  
will exclude entire  
parameter space

this analysis: Bayesian style  
CDF analysis: frequentist  
EWPD: electroweak

